## n <br> Corbettmoths

## Equipment

1. A black ink ball-point pen.
2. A pencil.
3. An eraser.
4. A ruler.
5. A pair of compasses.
6. A protractor.
7. A calculator

## Guidance

1. Read each question carefully.
2. Don't spend too long on one question.
3. Attempt every question.
4. Check your answers seem right.
5. Always show your workings

## Information

1. Time: 1 hour 30 minutes
2. The maximum mark for this paper is 80 .
3. You may use tracing paper.

| Question | Mark | Available |
| :---: | :---: | :---: |
| 1 |  | 6 |
| 2 |  | 3 |
| 3 |  | 4 |
| 4 |  | 4 |
| 5 |  | 3 |
| 6 |  | 4 |
| 7 |  | 3 |
| 8 |  | 4 |
| 9 |  | 6 |
| 10 |  | 3 |
| 11 |  | 3 |
| 12 |  | 3 |
| 13 |  | 3 |
| 14 |  | 6 |
| 15 |  | 4 |
| 16 |  | 5 |
| 17 |  | 3 |
| 18 |  | 4 |
| 19 |  | 4 |
| 20 |  | 5 |
| Total |  | 80 |

1. $\xi=\{$ odd numbers less than 32$\}$
$A=$ multiples of 3
$B=$ multiples of 5
(a) Complete the Venn diagram

(4)

One of the numbers is selected at random.
(b) Write down $\mathrm{P}(\mathrm{A} \cap \mathrm{B})$
2. Solve the simultaneous equations

$$
\begin{aligned}
& 3 x-y=23 \\
& 2 x+3 y=8
\end{aligned}
$$

Do not use trial and improvement

$$
x=
$$

$\qquad$ $y=$ $\qquad$
3. The table shows the ages of an under-21 rugby squad.

| Age | Frequency |
| :---: | :---: |
| 18 | 5 |
| 19 | 5 |
| 20 | 9 |
| 21 | 4 |

(a) Find the median age.

Courtney says that the mean age and median age are the same.
(b) Is Courtney correct?

You must give a reason for your answer.
4. Harley sold 380 ice creams.

He sold only vanilla, chocolate, strawberry and honeycomb ice creams. $45 \%$ of the ice creams are chocolate.

The ratio of vanilla ice creams to strawberry ice creams to honeycomb ice creams is 1:2:8.

Work out how many more chocolate ice creams are sold than honeycomb ice cream.
5. Shown below are two identical regular polygons and an equilateral triangle.


Calculate the number of sides each regular polygon has.
6. Material A has a density of $5.8 \mathrm{~g} / \mathrm{cm}^{3}$. Material B has a density of $4.1 \mathrm{~g} / \mathrm{cm}^{3}$.

377 g of Material A and 1.64 kg of Material B form Material C.
Work out the density of Material C.
7.


Calculate the size of angle BAC.
$\qquad$
8. Shown is a square and a circle.


Each vertex of the square is on the circumference of the circle.

The area of the circle is $81 \mathrm{~cm}^{2}$
Find the area of the shaded region.
Give your answer to 4 significant figures.
9. The functions $f(x)$ and $g(x)$ are given by the following:

$$
\begin{aligned}
& f(x)=8-3 x \\
& g(x)=4 x
\end{aligned}
$$

(a) Calculate the value of $g f(3)$
(b) Solve the equation $g f(x)=80$
10. Charlotte invests $£ 5000$.

The bank pays $10 \%$ interest for the first year and then y\% every year after that.
After three years, Charlotte has $£ 5610.55$
Calculate y.
11. A food standards inspector is going to visit 3 establishments in one day. In the town, there are 40 restaurants and 12 cafes.

He writes a list of the three different establishments, and the order will either be:
Cafe
Restaurant
Restaurant

| Restaurant |
| :--- |
| Cafe |
| Cafe |

How many possible lists could he write?
12. The points $D, E, F$ and $G$ lie in a straight line.

$$
\begin{aligned}
& \mathrm{DE}: E G=1: 4 \\
& \mathrm{DF}: F G=9: 11
\end{aligned}
$$

Work out DE : EF : FG
(3)
13.


The region labelled R satisfies three inequalities.
State the three inequalities
$\qquad$
$\qquad$
$\qquad$
14. (a) Simplify fully

$$
\frac{5 x^{2}-13 x-6}{x^{2}-9}
$$

(b) Make $m$ the subject of the formula

$$
y=\frac{m+4}{m+5}
$$

$$
\mathrm{m}=
$$

15. 



The area of the triangle is $90 \sqrt{3} \mathrm{~cm}^{2}$

Work out the value of $x$.

$$
x=
$$

(4)
16. Using $x_{n+1}=-3-\frac{2}{x_{n}^{2}}$
with $x_{0}=-3.5$
(a) find the values of $x_{1}, x_{2}$ and $x_{3}$

$$
\begin{aligned}
& x_{1}= \\
& x_{2}= \\
& x_{3}=
\end{aligned}
$$

(b) Explain the relationship between the values of $x_{1}, x_{2}$ and $x_{3}$ and the equation $x^{3}+3 x^{2}+2=0$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
17. The curved surface area of a cone is given by the formula

$$
A=\pi r l
$$

where $A$ is the curved surface area $r$ is the radius of the base of the cone and $I$ is the slant height

Given $\quad A=220 \mathrm{~cm}^{2}$ correct to 3 significant figures, and $r=8 \mathrm{~cm}$ correct to 1 significant figure.

Calculate the upper bound for I.
18.


Find the values of $x$ and $y$
19. Solve the inequality $2 x^{2}+9 x+10>0$
20. The circle $C$ has equation $x^{2}+y^{2}=4$

The circle is reflected in the line $y=2$ to give circle $D$
Circle $D$ is translated by the vector $\binom{-1}{0}$ to give circle $E$
(a) Draw a sketch of circle E
(b) Write down the coordinates of the centre of circle E

## $(\ldots . . . . . ., \ldots . . . .$.

(c) Work out the coordinates of points where circle E meets the y-axis
$\qquad$
$\qquad$

