

GCSE MATHEMATICS 8300/2F

Foundation Tier

Paper 2 Calculator

Shadow paper based on June 2023 paper

Mark scheme

June 2023

Version: 1.0

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

Copyright information

AQA retains the copyright on all its publications. However, registered schools/colleges for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to schools/colleges to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Copyright © 2023 AQA and its licensors. All rights reserved.

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

Μ	Method marks are awarded for a correct method which could lead to a correct answer.
A	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≼ value < b
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles.

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

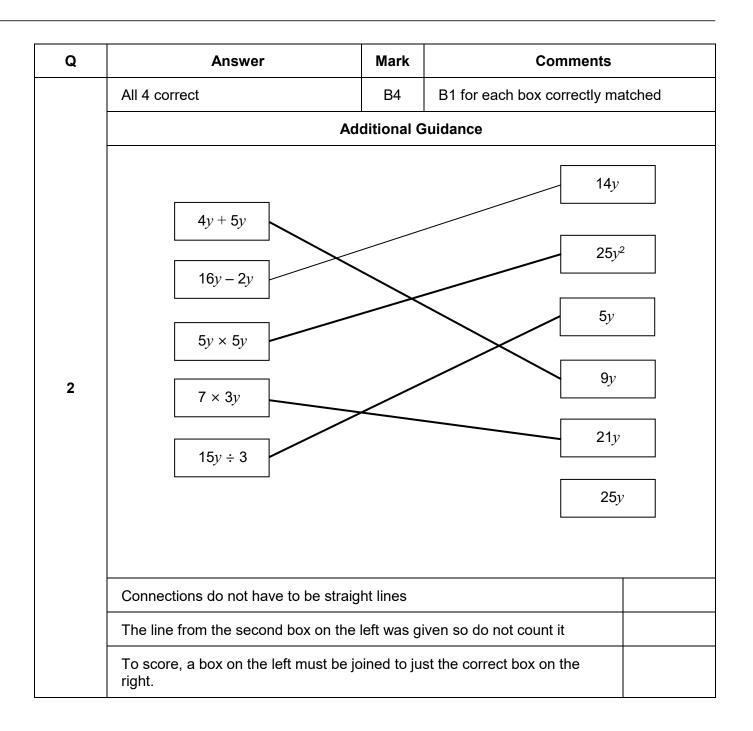
Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Q	Answer	Mark	Comments	
	40	B1		
1(a)	Additional Guidance			
	Mark the answer line. If this is blank, the answer may be seen on the diagram			

Q	Answer	Mark	Comments	
	-8	B1		
1(b)	Additional Guidance			
	Mark the answer line. If this is blank, the answer may be seen on the diagram			



Q	Answer	Mark	Comments		
	A and (A =) 14 and (B =) 12	B2	B1 (A =) 14 or (B =) 12 14 and/or 12 may be on the accept 140 and 120	diagram	
	Additional Guidance				
3(a)	Ignore reference to areas of any shapes and perimeters of the other shapes		erimeters of the other shapes		
	Ignore units, including for 140 and 12	20			
	If answer line blank, accept A clearly	indicated	in working		
	Accept 14 on the answer line in place	B2			

Q	Answer	Mark	Comments
3(b)	E	B1	

Q	Answer	Mark	Comments
3(c)	B and D	B1	either order

Q	Answer	Mark	Comments
	Any correct reflection of shape with corresponding mirror line shown	B2	B1 any correct reflection of shape with no or incorrect mirror line
	Ade	ditional G	Guidance
	Mark intention for mirror line and sha		
3(d)	Ignore internal lines		
	For B2, if there is more than one sha apply the rules of choice	pe and/o	r more than one mirror line,
	For B1, any one correct reflection of t shapes) will score B1	(even with other incorrect	

Q	Answer	Mark	Comments		
	(3, 2)	B1	accept $\begin{pmatrix} x & y \\ (3, 2) \end{pmatrix}$		
	Additional Guidance				
4(a)	Mark the answer line. If this is blank, diagram but must be the coordinates				
	Do not allow x and y within the coordinates eg $(3x, 2y)$				

Q	Answer	Mark	Comments	
	$(x, -4)$ where $x \neq 3$	B1	accept eg $\begin{pmatrix} x & y \\ 6, & -4 \end{pmatrix}$	
4(b)	Ad	ditional G	Guidance	
	Do not allow <i>x</i> and <i>y</i> within the coord	inates eg	(6x, -4y)	B0

Q	Answer	Mark	Comments	
	5 ÷ 0.65 or 500 ÷ 65 or 7.69() or 7.7 or 65 × 7 or 455 or 0.65 × 7 or 4.55 or 65 × 8 or 520 or 0.65 × 8 or 5.2(0)	M1	oe eg build up or build down	
	7	A1		
5(a)	Additional Guidance			
	Incorrect work seen is A0 eg $65 \times 7 = 455$ and $65 \times 8 = 530$ Answer 7			
	Do not allow 5 ÷ 65 or 500 ÷ 0.65 ι	unless rec	overed	
	Build up must be fully correct method, no errors, 65, 130, 195, 260, 325, 390, 455, (520)			
	Build down must be fully correct meth 110, 45	nod, no er	rors, 435, 370, 305, 240, 175,	

Q	Answer	Mark	Comments
	Alternative method 1 Comparing t	he cost of	40 bottles
	5.5 × 0.1 or 0.55 or 1 – 0.1 or 0.9	M1	oe eg 5.5 \div 10 discount or multiplier for shop D implied by 5.5 \times 5 \times 0.1 or 2.75 or 4.95
	(5.5 – their 0.55) × 5 or 5.5 × their 0.9 × 5 or 4.95 × 5 or 24.75	M1dep	oe eg 27.5(0) × 0.9 or 27.5(0) – 2.75 shop D
	13 × 2 or 26	M1	oe shop F
	D with 24.75 and 26 seen	A1	ое
	Alternative method 2 Comparing t	he cost of	1 bottle
	5.5 × 0.1 or 0.55 or 1 – 0.1 or 0.9	M1	oe eg 5.5 \div 10 discount or multiplier for shop D implied by 5.5 \div 8 \times 0.1 or 0.06(875) or 4.95
5(b)	(5.5 – their 0.55) ÷ 8 or 5.5 × their 0.9 ÷ 8 or 4.95 ÷ 8 or 0.61(875) or 0.62	M1dep	oe eg 0.68(75) × 0.9 or 0.68(75) – 0.06(875) shop D
	13 ÷ 20 or 0.65	M1	oe shop F
	D with 0.61(875) or 0.62 and 0.65 seen	A1	ое
	Alternative method 3 Comparing t	he cost of	20 bottles
	5.5 × 0.1 or 0.55 or 1 – 0.1 or 0.9	M1	oe eg 5.5 \div 10 discount or multiplier for shop D implied by 5.5 \times 2.5 \times 0.1 or 1.375 or 4.95
	(5.5 – their 0.55) × 2.5 or 5.5 × their 0.9 × 2.5 or 4.95 × 2.5	M1dep	oe eg 16.5 × their 0.9 or 16.5 – 1.65 shop D
	D with 12.37(5) or 12.38 (and 13) seen	A2	A1 12.37(5) or 12.38 oe

Question 5(b) continues on the next page

	Additional Guidance					
		narks may be awarde even if this is seen an			orrect	
	Use the s	scheme that favours t	he student			
	eg 0.62 a	and 0.65 followed by 2	24.8(0) and 26(.00) a	and D (mark by Alt 2	2) M3A1	
	All schem for up to	nes can be oe in peno 3 marks	ce and allow work in	a mix of pounds or	pence	
	Condone	Condone eg answer 24.75 with 26 seen			M3A1	
5(b) cont	For 0.1 \times 5.5, accept 10% \times 5.5 but do not accept 10% of 5.5 unless recovered					
	Allow var	iations				
	eg Shop D £27.5(0), Shop F £26,					
	Shop D is £1.50 more but the discount is £2.75			M1M1		
	Shop D c	heaper			A1	
		e student compares e evant figures given be		ottles apply the prir	nciples of Alt 2 –	
	Shop	Cost of 2	Cost of 4	Cost of 5	Cost of 80	
	D	1.23(75) or 1.24	2.47(5) or 2.48	3.09(375)	49.5(0)	
		1	1			

Q	Answer	Mark	Comments			
6	All five extra sets ie WY or YW but not both and WZ or ZW but not both and XY or YX but not both and XZ or ZX but not both and YZ or ZY but not both	B2	list in any order B1 any three or four of the five correct			
	Additional Guidance					
	Mark the grid unless blank					
	Ignore extras, repeats and reversals	not for B2				

2.6(0)

52(.00)

3.25

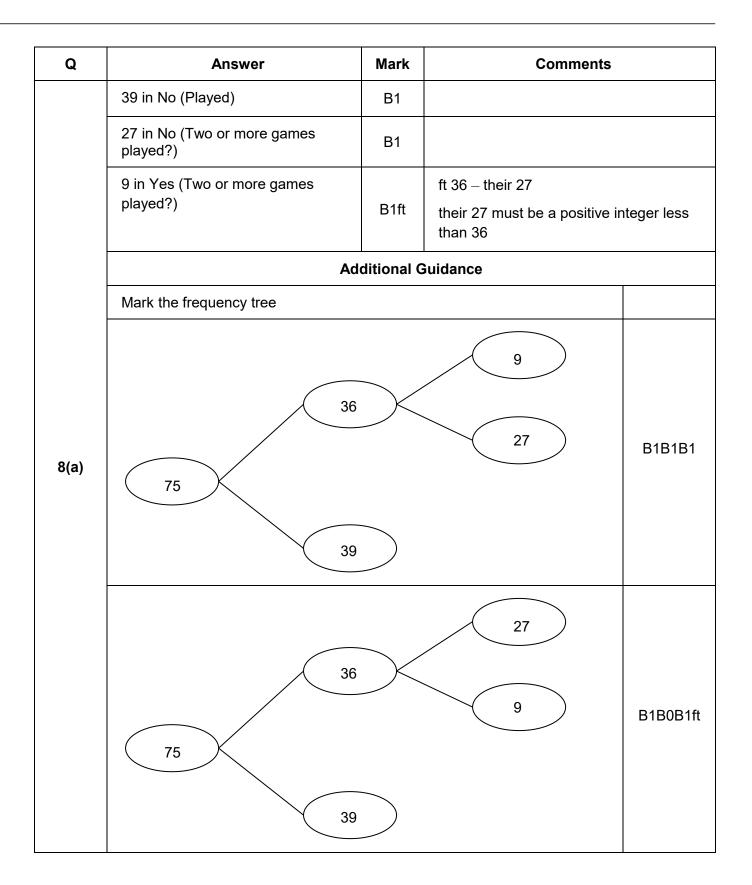
F

1.3(0)

Q		Answe	r			Mark	Comments	
	Two even and two odd numbers and the numbers all different and the sum of the four numbers is 38			8	B2	any order B1 two even and two odd nu and the sum of the four numbers or the numbers all different and the sum of the four numbers or two even and two odd number and the numbers all different and the sum of the four numbers	four numbers is 38 I different four numbers is 38 wo odd numbers I different	
7(a)	8 + 7	10 +	9	+	11			B2
	20 + 8	3 +	5	+	5	(not	all different)	B1
	8 + 1	0 +	14	+	6	(no	odds)	B1
	20 + 8	3 +	13	+	7	(not	t 38 but in range)	B1
	11 + 8	8 +	11	+	12	(not	all different and not 38)	B0
	5 + 7	7 +	11	+	17	(no	evens and not 38)	B0
	Negatives are	e accept	able fo	or B1	or B2			
	0 is an even r	number f	for B1	or B	2, but	a blank b	box does not imply 0	
	Fractions and sum to 38 for		imals a	are a	ccept	able for fo	our different numbers that	
	Mark the boxes							

Q			Answer	Mark	Comments	
7(b)	5 or 10] ×	8	B2	either order B1 uses a factor of 24 and the product of the two numb or uses a factor of 50 and the product of the two numb or the product of the two numb	ers is [32, 48]
7(6)				Additional (Guidance	
	8	×	6			B1
	7	×	5			B1
	40	×	1			B1
	2	×	20			B1
	Fractio	ons a	and/or decimals	are acceptable for	non-factors for B1	
	Mark t	he b	ooxes			

Q			An	wer	Mark	Comments	
	64	÷	2		B2	B1 any square number > 1 or any prime number	
				Ad	ditional G	Guidance	
	Allow	squa	ares to	be written in index f	orm for B2	2 or B1 eg	
7(c)	8 ²	÷	2				B2
	2	÷	64				B1
		÷	9				B1
	128	÷	4				B1
	Mark the boxes						



Q	Answer	Mark	Comments				
	Alternative method 1	Alternative method 1					
	0.63 × 75 or 47.2(5) or 47.3	M1	ое				
	48	A1					
	Alternative method 2	L					
	$\frac{47}{75} = 0.62()$		other trials can be ignored				
	or	M1					
8(b)	$\frac{48}{75} = 0.64$						
	48	A1					
	Additional Guidance						
	Answer only 48		M1A1				
	0.64 × 75 = 48 with answer 48 (without seeing 0.63 × 75 or 47.2) M0A0					
	For 0.63×75 , accept $63\% \times 75$ by recovered	cept 63% of 75 unless					

Q	Answer	Mark	Comments			
	9×2 or 18		oe			
	or	M1				
	$16 \times (12 - 2)$ or 16×10 or 160					
9(a)	178	A1				
	Additional Guidance					
	178.00(p)			M1A1		
	178.0			M1A0		

Q	Answer	Mark	Comments		
	Alternative method 1 Works in min	or hrs for	11 episodes and 1 episode		
	11 × 40 or 440 or $11 \times \frac{40}{60}$ or $\frac{440}{60}$	M1	oe eg 11 × $\frac{4}{6}$ or $\frac{44}{6}$ or $\frac{22}{3}$ or 7.3()		
	60 + 22 or 82 or $\frac{82}{60}$ oe fraction or 1.3(6)	M1	522 or 8.7 implies M1M1		
	8 hours 42 minutes	A1	SC2 6h2min		
	Alternative method 2 Works in min	or hrs for	11 episodes and converts to hrs and min		
9(b)	11 × 40 or 440 or 11 × $\frac{40}{60}$ or $\frac{440}{60}$	M1	oe eg 11 × $\frac{4}{6}$ or $\frac{44}{6}$ or $\frac{22}{3}$ or 7.3() implied by 7 h 20 min		
	7 h 20 min	M1	ft conversion of their 440 to hours and minutes if their 440 > 60 or their $\frac{440}{60}$ to hours and minutes if thei $\frac{440}{60} > 1$		
	8 hours 42 minutes	A1	SC2 6h2min		
	Ad	ditional G	Guidance		
	4 h 40 min + 1 h 22 min = 6 h 2 min		SC2		

Q	Answer	Mark	Comments		
	1440 ÷ 3 (× 2) oe or 480 (× 2) M1				
	960	A1			
	Additional Guidance				
10(a)	$\frac{960}{1440}$ on answer line	M1A0			
	Condone 960 out of 1440	M1A1			
	For 0.66() × 1440, accept 66.()% 1440 unless recovered				

Q	Answer	Mark	Comments	
	7 11	B1	oe fraction	
10(b)	Ade	ditional G	Buidance	
	Conversion to decimal or percentage			B0

Q	Answer	Mark	Comments		
	114 ÷ 150 (× 100) or 0.76	M1	oe		
10(0)	76	A1	SC1 24		
10(c)	Additional Guidance				
	Build-up methods must be correct or show correct method for each step				

Q	Answer	Mark	Comments			
	5 in H only	B1				
	10 in (M U H)'	B1ft	ft 15 – their 5 their 5 must be < 15			
11(a)	Additional Guidance					
	11 in H only			В0		
	10 in (M U H)'			B1		
	11 in H only			B0		
	4 in (M U H)'			B1ft		

Q	Answer	Mark	Comments	
	$\frac{6}{60}$ or $\frac{1}{10}$ or 0.1 or 10%	B1	oe fraction	
	Additional Guidance b) Ignore conversion attempt to decimal, fraction or percentage (but not ratio) after correct probability seen			
11(b)				
	Do not allow eg 6 in 60 or 6 out of 60 unless the correct probability seen			
	Do not allow ratio			
	Ignore words if correct probability seen			

Q	Answer	Mark	Comments				
	Valid explanation	B1	eg needs brackets around 45 – 17				
	Ad	ditional C	Buidance				
	Any calculations shown must be corr	ect					
	Ignore irrelevant, non-contradictory s	tatements					
	It gives 40.75 and it should be 7			B1			
	(It gives the wrong answer,) it should	be 7		B1			
	He shouldn't divide (by 4) first			B1			
	He needs brackets around the takea	way		B1			
	He needs to subtract first						
	He should do 45 – 17 and then divide	B1					
11(c)	$(45-17) \div 4$ (may correct the give	B1					
	$\frac{45-17}{4}$ (implies the brackets)	B1					
	This gives 40.75 (or 163) when he ne	B1					
	$45 - 17 = 28$ $28 \div 4 = 7$ (needs to	В0					
	This gives 40.75 (or 163) which is too 28)	omuch (needs to compare with 7 or	В0			
	He hasn't used BIDMAS			В0			
	It gives the wrong answer			В0			
	45 – 17 ÷ 4 = 7	В0					
	45 – 17 ÷ 4 = 40.75			В0			
	He needs brackets	В0					

Q	Answer	Mark	Comments			
12	Ticks Both of them and gives valid reason for Sune eg references both values being divided (or multiplied) by 3 and gives valid reason for Peter eg references both values being divided (or multiplied) by 5	B2	oe valid reason eg1 $6 \div 2 \times 5 = 15$ and $6 \div 15$ or eg2 $6 \div 15 = 0.4$ and $2 \div 5$ and $1.2 \div 3 = 0.4$ B1 ticks Sune only and gives valid reason for S or ticks Peter only and gives valid reason for P or ticks Both of them and gives valid reason for S	5 = 0.4 Sune Peter		
	Ad Accept a build-up method to imply m eg all three of 2 : 5 and 4 : 10 and 6 : or all five of 1.2 : 3 and 2.4 : 6 and 3.					
	Condone eg 2:5 \times 3 = 6:15 to imply both values are multiplied by 3			B0		
		2 is a factor of 6 and 5 is a factor of 15 (with no reference to \times 3) 6 : 15 = 2 : 5 or $\frac{6}{15} = \frac{2}{5}$ (not evaluated to 0.4 or shown \div 3)				
	6 : 15 simplifies to 2 : 5 and 1.2 : 3 (v	erence to ÷ 3 or ÷ 5)	B0			
	2 : 5 and 1.2 : 3 are both equivalent t × 5)	with no reference to \times 3 or	В0			

Q	Answer	Mark	Comments			
	Correct method or evaluation for the 15% or the 25% or correct multiplier for the increase or the decrease seen	M1	eg 40 × 0.15 or 6 or 64 × 0.25 or 16 or 1.15 or 0.75 oe			
	Correct method or evaluation for either calculation	M1dep	eg 40 + 40 × 0.15 or 46 or 64 × 0.75 or 48			
	Correct method or evaluation for both calculations	M1dep				
	48 with 46 seen	A1	oe eg 64 decreased by 25% wi seen	th 48 and 46		
13	Additional Guidance					
	40 × 1.15 or 46		M1M1			
	64 × 0.75 or 48		M1M1			
	40 × 1.15 or 46 and 64 × 0.75 or	M1M1M1				
Build-up methods must be correct or show correct method for ea eg 1 $10\% = 4$, $5\% = 2$, $15\% = 6$ eg 2 $10\% = 6.4$, $5\% = 6.4 \div 2 = 3.2$, $25\% = 17.2$ (error in build-				M1 M1		
	method shown for that step) eg 3 $10\% = 6.4$, $5\% = 3.6$, $25\% = 1$ shown for that step)	MO				
	48 and 46 seen and 48 chosen by e	M3A1				
	For 40×0.15 , do not accept 40×15					

Q	Answer	Mark	Comments		
	7(2x+3y)	B1			
	Ade	ditional G	Guidance		
	Condone missing final bracket ie $7(2x + 3y)$				
14	Allow multiplying back out to check th	er			
	Further incorrect work after a correct	response	is B0		
	eg 7(2x+3y) = 35xy			B0	
	$7(x^2 + y^3)$				
	$7 \times (2x + 3y)$			В0	

Q	Answer	Mark	Comments	
	-1, 0, 1, 2, 3	B2	any order B1 four correct and none inc or five correct and one incorrec	
15	Ad	Guidance		
15	-1, 0, 1, 2			B1
	-1, 0, 1, 2, 3, 4			B1
	-1, 1, 2, 3			B1
	-1, 1, 2, 3, 4			В0

Q	Answer	Mark	Comments		
	5n+2 or $2+5n$	oe eg 7 + (5 <i>n</i> − 5) B1 5 <i>n</i> (+ …) or 5 <i>n</i> (− …)			
	Ad	ditional C	Guidance		
	Ignore LHS of formula given eg $T_n =$	5 <i>n</i> + 2		B2	
	Condone $n = 5n + 2$ or <i>n</i> th term $= 5n + 2$ Allow a multiplication sign eg $5 \times n + 2$ or $n \times 5 + 2$				
16	Allow other variables eg $5x + 2$			B2	
	5 <i>x</i>			B1	
	n5			B1	
	<i>n</i> 5 + 2			B1	
	5 <i>n</i> th + 2			B1	
	5 <i>n</i> th				
	5n + 2n			В0	

Q	Ans	wer		Mark		Comments		
	35 × 9 or 315			M1		of 2p coins embedded		
	35 × 9 × 2 or 315 × 2 or 630 or 6.3(0)			M1dep	oe value of 2p coins implied by 980 or 9.8(0)			
	14.3(0) – their 6.3 or 1430 – their 630 – or 4.5(0) or 450			M1dep	oe value of 5p coins implied by 6.3 : 4.5 oe ratio not in simplest form or 4.5 : 6.3 oe ratio			
	7:5			A1	accept 1.4 : 1 or $\frac{7}{5}$: 1 or $1\frac{2}{5}$: 1 or 1:0.71() or 1: $\frac{5}{7}$			
17	Additional Guidance							
	Up to M3 may be answer, even if th	er or incorrect						
	Allow working in pence or pounds throughout							
	Must work consist	ark (or recover)						
	Ignore units in the ratio eg 7p : 5p or £1.40 : £1						M3A1	
	630 may be seen eg 630 : 350 or 6		ith the va	lue of the	10p coins	3	M2	
	450 may be seen in a ratio with the value of the 10p coins eg 450 : 350 or 4.5 : 3.5					3	М3	
	For information:	Coin	10p	2р	5р			
		Number	35	315	90			
		Value	£3.50	£6.30	£4.50			

Q	Answer				Mark			Commen	Its	
	All values		B2	B1	1 or 2 row	s correct				
		Additional Guidance								
		1	2	3		4	5	6		
18(a)	5 <i>x</i>	5	10	15		20	25	30		B2
	8 <i>x</i>	8	16	24	;	32	40	48		DZ
	x ²	1	4	9	,	16	25	36		

Q	Answer	Mark	Comments		
	5 18 or 0.27(7) or 0.28 or 27(.7)% or 28%	B1ft	oe fraction, decimal or perce ft their table with ≥ 12 values must be using 18 for the tota possible scores	6	
	Additional Guidance				
18(b)	Ignore simplification or conversion at seen	tempt (not	t ratio) after correct probability		
	Ratio answer eg 5 : 18, even alongsi	de a corre	ct probability is B0		
	ft decimals or percentages must be correct to the same accuracy as in the scheme				
	eg 8 winning values in their table				
	$\frac{8}{18}$ or 0.44(4) or 44(.4)%		B1ft		

Q	Answer	Mark	Comments	
	756 × their $\frac{5}{18}$	M1	oe ft their probability from (b) or if no probability in (b), ft their table with ≥ 12 values where 0 < their probability < 1 probabilities, if rounded in (c), must be truncated or rounded to at least 2 sf	
	210	A1		
	Ad	ditional G	Guidance	
	Answer 210	M1A1		
	$\frac{210}{756}$ on answer line	M1A0		
10()	Condone 210 out of 756	M1A1		
18(c)	Do not treat estimating by rounding a eg1 800 used instead of 756 eg2 (b) 0.27 (c) 0.3×756 (round eg3 (b) 0.3 (c) 0.3×756 (follow	in (c) for the probability) M0A0		
	Do not allow ft for a ratio from (b) but	eir (a) instead		
	For 0.27 × 756, accept 27% × 756 burne recovered	accept 27% of 756 unless		
	The method mark may be implied by the nearest integer or rounded up to eg1 (b) $\frac{6}{16}$			
	(c) 283.5 or 283 or 284 (correct f	implied using (b)) M1A0		
	eg2 (a) completed table has 6 winnin (c) 252 (correct ft method implie			

Q	Answer	Mark	Comments		
	360 ÷ 6 or 120 seen	M1	oe eg 60 × 6 = 360 or $180 - \frac{(6-2) \times 180}{6}$ may be on diagram		
19(a)	60	A1			
	Additional Guidance				
	M1 may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts				
	60 seen but not chosen as answer, e	ed to the wrong angle	11A0		

Q	Answer	Mark	Comments
19(b)	It is more than the answer to part (a)	B1	

Q	Answer	Mark	Comments	
	$\begin{pmatrix} 5\\ -4 \end{pmatrix}$	B2	B1 $\begin{pmatrix} 5 \\ \end{pmatrix}$ or $\begin{pmatrix} \\ -4 \end{pmatrix}$ SC1 $\begin{pmatrix} -5 \\ 4 \end{pmatrix}$	
	Additional Guidance			
	$(5, -4)$ or $\begin{pmatrix} -4\\5 \end{pmatrix}$			
	Ignore words if a vector is also seen			
	eg1 Reflection $\begin{pmatrix} 5\\ -4 \end{pmatrix}$			B2
20	eg2 5 right 4 up and $\begin{pmatrix} 5\\4 \end{pmatrix}$			B1
	eg3 5 right 4 down			B0
	eg4 Rotate 5 left and 4 up and $\begin{pmatrix} -5\\4 \end{pmatrix}$			SC1
	Condone any type of brackets			
	Condone missing brackets for B2 or B1 or SC1 but must have two numbers in a column			
	Condone 'fraction line' for B2 or B1 or SC1 but must have two numbers in a column			
	$ \begin{pmatrix} 5x \\ -4y \end{pmatrix} \text{ or } \begin{pmatrix} x5 \\ -y4 \end{pmatrix} \text{ or } \begin{pmatrix} x+5 \\ y-4 \end{pmatrix} \text{ or } \begin{pmatrix} x \\ 2 \end{pmatrix} $	5 right down) c	or $\begin{pmatrix} 5 \\ 4 \\ d \end{pmatrix}$ or $\begin{pmatrix} 5 \\ 4 \\ \downarrow \end{pmatrix}$	В0

Q	Answer	Mark	Comments	
	Alternative method 1 Compares 80% of volume of hemisphere with volume of water			
	$rac{4}{3}$ $ imes$ π $ imes$ 9 ³ or 972 π		oe eg $\frac{4}{3}\pi \times 729$	
	or [3044, 3054] or	M1	allow without any multiplication signs eg $\frac{4}{3}\pi 9^3$	
	$\frac{2}{3} \times \pi \times 9^3$ or 486 π		3	
	or [1522, 1527]			
	0.8 × their 486π or 388.8π or [1217, 1222]	M1dep	oe 0.8 × their [1522, 1527] or $\frac{1944}{5}\pi$	
			must be using volume of hemisphere	
	185 × 7 or 1295	M1	ое	
	[1217, 1222] and 1295 and Yes	A1	ое	
21	Alternative method 2 Works out volume of water as proportion of volume of hemisphere			
	$\frac{4}{3}$ × π × 9 ³ or 972 π		oe eg $\frac{4}{3}\pi \times 729$	
	or [3044, 3054]		allow without any multiplication signs	
	or	M1	eg $\frac{4}{3}\pi 9^3$	
	$\frac{2}{3} \times \pi \times 9^3$ or 486 π			
	or [1522, 1527]			
	185 × 7 or 1295	M1	Oe	
	their 1295 ÷ their 486 π		oe eg their 1295 ÷ their [1522, 1527]	
	or [0.84, 0.86]	M1dep	or 85%	
			dep on M2	
			must be using volume of hemisphere	
	[84, 86](%) and Yes	A1	oe eg 0.85 and 0.8 and Yes	

Question 21 continues on the next page

	Alternative method 3 Works out time to fill 80% of volume of hemisphere		
21 cont	$\frac{4}{3} \times \pi \times 9^3$ or 972π or [3044, 3054] or $\frac{2}{3} \times \pi \times 9^3$ or 486π or [1522, 1527]	M1	oe eg $\frac{4}{3}\pi \times 729$ allow without any multiplication signs eg $\frac{4}{3}\pi 9^3$
	0.8 × their 486π or 388.8π or [1217, 1222] or their 486π ÷ 185 or [8.1, 8.3]	M1dep	oe 0.8 × their [1522, 1527] or $\frac{1944}{5}\pi$ or their [1522, 1527] ÷ 185 must be using volume of hemisphere
	0.8 × their 486π ÷ 185 or 0.8 × their [1522, 1527] ÷ 185 or [6.5, 6.61]	M1dep	oe their [1217, 1222] ÷ 185 or 0.8 × their [8.1, 8.3]
	[6.5, 6.61] and Yes	A1	oe

Question 21 continues on the next page

	Additional Guidance			
	Up to M3 may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts			
	Allow 1.33() for $\frac{4}{3}$			
	Allow 0.66() or 0.67 for $\frac{2}{3}$			
	π may be seen as [3.14, 3.142] eg Alt 1 $\frac{2}{3} \times 3.14 \times 9^3$	M1		
	If a number (or calculation) in terms of π is seen but π is subsequently omitted, treat as a miscopy for M marks			
21	eg Alt 1			
cont	486π			
	$0.8 \times 486 = 388.8$	M1dep		
	185 × 7 = 1295 Yes	M1A0		
	Yes cannot be implied by inequalities			
	Alts 1 and 2			
	$185 \mathrm{cm}^3 \times 7$ seen is M1 even if evaluated incorrectly			
	$185^3 \times 7$ seen is M0 unless recovered to 1295			
	Do not allow misreads of the given formula unless recovered			
	eg1 using 9 ² instead of 9 ³			
	eg2 using $\frac{3}{4}$ instead of $\frac{4}{3}$			
	For 0.8 × their 486 π , do not accept 80% × their 486 π unless recovered			

Q	Answer	Mark	Comments	
	9 ÷ 4 or 13.5 ÷ 6 or $\frac{9}{4}$ or $\frac{13.5}{6}$ or 2.25 or 6 ÷ 4 or 13.5 ÷ 9 or $\frac{6}{4}$ or $\frac{13.5}{9}$ or 1.5	M1	oe use of a valid pair of side appropriate calculation or va eg 4 ÷ 9 or 0.44() or 4 ÷ 6 or 0.66()	
	9 ÷ 4 = 13.5 ÷ 6 or $\frac{9}{4} = \frac{13.5}{6}$ or 6 ÷ 4 = 13.5 ÷ 9 or $\frac{6}{4} = \frac{13.5}{9}$	A1	oe showing sides are in prop eg $4 \div 9 = 6 \div 13.5$ or $\frac{4}{6} = \frac{9}{13.5}$	portion
	Additional Guidance			
	For A1 equating may be implied by two calculations or two fractions with correct evaluation			
	eg $9 \div 4 = 13.5 \div 6$ is implied by $9 = 4 \times 2.25$ and $13.5 = 6 \times 2.25$		M1A1	
22	For A1 equating may be implied by calculations eg1 $9 \div 4 = 13.5 \div 6$ is implied by $9 \div 4 = 2.25$ and $6 \times 2.25 = 13.5$ eg2 $9 \div 4 = 13.5 \div 6$ is implied by $\frac{9}{4} \times 6 = 13.5$			M1A1 M1A1
	$4 \times 13.5 = 9 \times 6$			M1A1
	$4 \times 13.5 = 54$ and $9 \times 6 = 54$			M1A1
	Non-contradictory working can be ignored eg correct response along with area calculations			M1A1
	Ignore words eg references to scale factors, enlargement, angles			
	Working on diagrams may be seen eg1 Arrows or lines from 4 to 9 and 6 to 13.5 with \times 2.25 on them eg2 Arrows or lines from 4 to 9 and 6 to 13.5 with 2.25 on them Arrows or lines must unambiguously link relevant numbers			M1A1 M1A0
	For 9 ÷ 4 or $\frac{9}{4}$ allow 9 : 4 etc			

Q	Answer	Mark	Comments	
	$ \begin{array}{c} 100 \times x \text{ or } 100x \text{ or } x \times 100 \text{ or} \\ x100 \\ \text{or} \\ x \div 60 \text{ or } \frac{x}{60} \text{ or } \frac{1}{60}x \text{ or } x\frac{1}{60} \\ \text{or} \\ 100 \div 60 \text{ or } \frac{100}{60} \end{array} $	M1	plasters per hour boxes per minute	
	$\frac{100x}{60} \left(=\frac{5x}{3}\right)$ or $100 \div 60 \times x \left(=\frac{5x}{3}\right)$	A1	oe showing 100 and 60 and eg $\frac{100 \times x}{60} \left(=\frac{5x}{3}\right)$ or $x\frac{10}{60}$ or $\frac{100}{60} \times x \left(=\frac{5x}{3}\right)$ or $100x \div 60 \left(=\frac{5x}{3}\right)$	
23	Ad	ditional G	Guidance	
	M1 may be awarded for correct work with no answer or incorrect answer, even if this is seen amongst multiple attempts			
	Do not allow M1 if only seen embedded in an incorrect expression or calculation eg $100x \times 5 = 500x$			MO
	$60 \times \frac{5x}{3} = 100x$ (M1 allowed as $100x$ is not embedded in an incorrect expression or calculation, A0 because using the given answer)			M1A0
	Condone $x = 100 \div 60$			M1A0
	$\frac{100x}{60} \left(=\frac{5x}{3}\right)$			M1A1
	$\frac{100}{60} = \frac{5}{3}$ and $\frac{5}{3} \times x \left(=\frac{5x}{3}\right)$			M1A1
	$\frac{100}{60} = \frac{5}{3}$ and $\frac{5x}{3}$			M1A0

Additional guidance for Question 23 continues on the next page

Q	Additional Guidance (continued)		
	No equivalents allowed for M1		
	Ignore units		
23	Condone 1.66() for $\frac{5}{3}$		
	Ignore non-contradictory working after M1A1 seen		