## AQA ${ }^{[ }$

# GCSE MATHEMATICS 

2023 PRACTICE PAPER SET 1 Higher Tier Paper 2
Mark Scheme

Version 1.1

Principal Examiners have prepared these mark schemes for specimen papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

Further copies of this Mark Scheme are available from aqa.org.uk

## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M | Method marks are awarded for a correct method which could <br> lead to a correct answer. |
| :--- | :--- |
| A | Accuracy marks are awarded when following on from a correct <br> method. It is not necessary to always see the method. This can <br> be implied. |
| B | Marks awarded independent of method. |
| ft | Follow through marks. Marks awarded for correct working <br> following a mistake in an earlier step. |
| SC | Special case. Marks awarded within the scheme for a common <br> misinterpretation which has some mathematical worth. |
| M dep method mark dependent on a previous method mark being |  |
| awarded. |  |$\quad$| A mark that can only be awarded if a previous independent mark |
| :--- |
| has been awarded. |

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

## Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

## Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then $M$ marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 6 | 2, 3 and 4 chosen | M1 | May be implied from a diagram |
|  | 24 | A1 |  |
|  |  |  |  |
| 7(a) | $4 \leqslant t<6$ | B1 |  |
| 7(b) | Alternative method 1 |  |  |
|  | $\begin{aligned} & 18+10+16+12 \text { or } 56 \text { and } \\ & 60 \times 0.9 \\ & \text { or } \\ & (18+10+16+12) \div 60 \times 100 \text { or } \\ & 93.3 \ldots \end{aligned}$ | M1 | oe |
|  | 56 and 54 and $Y e s$ or 93(.33)(\%) and Yes | A1 |  |
|  | Alternative method 2 |  |  |
|  | $\begin{aligned} & 4 \text { and } 60 \times 0.1 \\ & \text { or } \\ & 4 \div 60 \times 100 \text { or } 6.66 \end{aligned}$ | M1 | oe |
|  | 4 and 6 and Yes or 6(.66)(\%) or 7(\%) and Yes | A1 |  |


| Q Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| 8(a) | Use of cos, or cos chosen, ie circled in SOHCAHTOA | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $\cos x=\frac{7}{12}$ <br> or $\sin x=\frac{\sqrt{12^{2}-7^{2}}}{12}$ <br> or $\tan x=\frac{\sqrt{12^{2}-7^{2}}}{7}$ $x=\cos ^{-1}\left(\frac{7}{12}\right)$ <br> or $x=\sin ^{-1}\left(\frac{\sqrt{12^{2}-7^{2}}}{12}\right)$ <br> or $x=\tan ^{-1}\left(\frac{\sqrt{12^{2}-7^{2}}}{7}\right)$ | M1 | oe |
|  | 54(.3...) | A1 |  |
| 8(b) | Use of tan or tan chosen eg circled TOA in SOHCAHTOA | M1 |  |
|  | $\tan 42=\frac{y}{35}$ or $\tan 48=\frac{35}{y}$ or $y=35 \tan 42$ <br> or $y=\frac{35}{\tan 48}$ | M1 | oe $\begin{aligned} & x=47.1 \ldots \text { and } 35^{2}+y^{2}=47.1^{2} \\ & 47.1 \cos 48 \text { or } 47.1 \sin 42 \end{aligned}$ |
|  | 31.5 (...) | A1 |  |


| 9 | $y^{2}-3 y+8 y-24$ | M1 | Allow 1 error |
| :--- | :--- | :---: | :--- |
|  | $y^{2}+5 y-24$ | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 10 | 8 and 80 | B1 |  |
|  | their $8 \times 10+$ their $80 \times 2$ <br> or $80+160$ <br> or 240 | M1 |  |
|  | their $240+155$ or 395 | M1 |  |
|  | their $395 \div 0.5$ - their 8 - their 80 or their $395 \times 2-$ their $8-$ their 80 or 790 - their 8 - their 80 or 702 | M1 |  |
|  | 702 | A1 |  |


| 11 | $\pi \times 30^{2} \times 160$ | M1 | $\begin{aligned} & 452389 \ldots \text { or } 144000 \pi \\ & {[452160,452389]} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | their $452389 \div 1000$ <br> or their $452389 \div 1000 \div 0.1$ | M1 | $\begin{aligned} & 452.3 \ldots \text { or } 144 \pi \\ & {[452.150,452.389]} \\ & 4523.8 \ldots \\ & {[4521.6,4524]} \end{aligned}$ |
|  | their $4523.89 \div 60(\div 60)$ <br> or $(60 \times 60)=3600$ <br> or $0.1 \times 60 \times 60$ or 360 | M1dep | $\begin{aligned} & 75.398 \ldots \text { or } 1.25 \ldots \\ & {[75.36,75.4] \text { or }[1.25,1.0526]} \end{aligned}$ |
|  | $[75.36,75.4] \text { and Yes }$ <br> or [1.25, 1.0526] and Yes or 3600 and 4523.8.... and Yes or 452.3... and 360 and $Y e s$ | A1 | oe |


| Q Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| 12 | Gradient is 4 | B 1 | Implied by $y=4 x \ldots$ |
| :---: | :--- | :---: | :--- |
|  | their $4 \times-1+c=1$ | M 1 |  |
|  | $y=4 x+5$ or $4 x-y+5=0$ <br> or $y-4 x-5=0$ | A 1 ft | ft their gradient |


| 13(a) | Fully correct of diagram using UCBs and $12,50,86,110,120$ $\begin{aligned} & (100,12)(120,50) \\ & (140,86)(160,110) \\ & (180,120) \end{aligned}$  | B3 | Ignore ( 80,0 ) <br> Ignore before 1st point and after last point <br> B2 for one error <br> eg constant plotting at mid class intervals with line joining points consistent plotting at lower bounds with line joining points <br> One error on cf values <br> eg 12, 50, 86, 110, 121 <br> Points not joined <br> B1 for 12, 50, 86, 110, 120 <br> or for bar chart indicating correct heights with no lines |
| :---: | :---: | :---: | :---: |
| 13(b) | Reads off at 130 | B1ft | ft their curve Must be increasing <br> $\pm \frac{1}{2}$ square tolerance |



| 15 | 3,1 and -2 | B3 | Any order <br> B1 for each |
| :---: | :--- | :--- | :--- |


| 16(a) | $g=4.5 y$ <br> or $g=k y \text { and } k=4.5$ | M1 | oe |
| :---: | :---: | :---: | :---: |
|  | 40.5 | A1 |  |
| 16(b) | $g \alpha \frac{1}{x^{3}}$ or $g=\frac{k}{x^{3}}$ | M1 | oe |
|  | $\begin{aligned} & 25=\frac{k}{2^{3}} \text { or } k=200 \\ & \text { or } g=\frac{200}{x^{3}} \end{aligned}$ | M1dep | oe |
|  | 0.2 | A1 | oe |
| 16(c) | A | B1 |  |


| 17 | Bars should not be of equal width <br> or horizontal scale is incorrect | B1 | oe |
| :---: | :--- | :---: | :--- |
|  | Vertical axis should be frequency <br> density <br> or heights of bars incorrect | B1 | oe |


| Q Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| 18 | Angle $B C D=2 x$ | M1 | Opposite angles of parallelogram are equal |
| :---: | :---: | :---: | :---: |
|  | Angle $F C E=360-90-90-2 x$ or Angle FCE $=180-2 x$ | M1 | oe <br> Angles at a point sum to $360^{\circ}$ |
|  | Angle CFE $=y$ <br> or Angle FCE $=180-2 y$ | M1 | oe <br> eg $2 y+F C E=180$ <br> Isosceles triangle |
|  | $180-2 x+y+y=180$ | M1 | oe <br> Angles in a triangle sum to $180^{\circ}$ |
|  | $\begin{aligned} & 2 y=2 x \\ & y=x \end{aligned}$ | A1 | All reasons must be stated |


| 19(a) | $\frac{7^{2}+3}{2 \times 7-7} \text { or } 7.42 \ldots$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | Substitutes their answer for $x$ or <br> 7.4052 | M1 |  |
|  | (7.42 and 7.4052 and answer) 7.4051 | A1 | Accept unrounded values for all but answer |
| 19(b) | -0.00019399 or -1.9399 $\times 10^{-4}$ | B1ft | ft their answer to (a) |
|  | Good approximation as the result is close to 0 | B1ft | ft the result of their calculation |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 20 | $x(x-11)+x+x+2+36=150$ | M1 |  |
|  | $x^{2}-9 x-112=0$ | A1 |  |
|  | $(x-16)(x+7)=0$ | M1 | oe $(x+a)(x+b)$ <br> where $a b=-112$ and $a+b=-9$ |
|  | their $16+$ their $16+2$ or 34 | M1 |  |
|  | $\frac{16}{34}$ | A1 | oe <br> SC 2 for $\frac{x}{2 x+2}$ |


| 21(a) | Draws a tangent at $t=4$ | B1 |  |
| :---: | :---: | :---: | :---: |
|  | $\frac{\text { change in speed }}{\text { change in time }} \text { for their tangent }$ | M1 |  |
|  | Correct answer for their tangent | A1ft |  |
| 21(b) | Attempts to work out area below straight lines | M1 | eg $4 \times 14$ or 56 and $\frac{1}{2} \times 6 \times 14$ or 42 |
|  | Attempts to work out estimate of area under the curve | M1 | $\begin{aligned} & \text { eg } \frac{1}{2} \times 14 \times 14 \text { or } 98 \\ & \frac{1}{2} \times 18 \times 14 \text { or } 126 \end{aligned}$ |
|  | their total distance $\div 24$ | M1 |  |
|  | Their answer worked out correctly with no errors in area below straight lines | A1 | Their area must be in the range [194, 224] |
| 21(c) | Correct box ticked with suitable comment | B1ft | ft their answer to part (b) <br> eg their (b) 194 <br> Underestimate ticked and triangle less than area under curve <br> their (b) 224 <br> Overestimate ticked and trapezium more than area under curve |


| Q Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| $\mathbf{2 2}$ | $(w+4)(w-4)$ | B 1 |  |
| :---: | :--- | :---: | :--- |
|  | $(w+1)(w+3)$ | B 1 |  |
|  | $(3 w+a)(w+b)$ | M 1 | $a b=4$ or $a+3 b=-13$ |
|  | A 1 |  |  |
| $\frac{\mathrm{Cw}-2}{w+1}$ | A 1 |  |  |

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